

Chapter.4
Moving Charges and Magnetism
Class – XII
Subject – Physics

4.1. A circular coil of wire consisting of 100 turns, each of radius 8.0 cm carries a current of 0.40 A. What is the magnitude of the magnetic field B at the centre of the coil?

Sol.

Given:

$$N = 100$$

$$R = 8\text{cm}$$

$$I = 0.4\text{ A}$$

By the formula

$$B = \frac{\mu_0 IN}{2R}$$

Substitution yields

$$B = 3.1 \times 10^{-4}\text{ T}$$

4.2. A long straight wire carries a current of 35 A. What is the magnitude of the field B at a point 20 cm from the wire?

Sol.

Given:

$$I = 35\text{ A}$$

$$x = 20\text{ cm}$$

Let us consider an Amperian loop of radius equal to x, i.e. 20 cm

Therefore by formula

$$B = \frac{\mu_0 I}{2\pi R}$$

Solving for B
 $B = 3.5 \times 10^{-5} \text{ T}$

- 4.3.** A long straight wire in the horizontal plane carries a current of 50 A in north to south direction. Give the magnitude and direction of B at a point 2.5 m east of the wire.

Sol.

Given:

$$I = 50 \text{ A}$$

$$R = 2.5 \text{ m}$$

Using the above formula

$$B = 4 \times 10^{-6} \text{ T}$$

Direction is vertical up.

- 4.4.** A horizontal overhead power line carries a current of 90 A in east to west direction. What is the magnitude and direction of the magnetic field due to the current 1.5 m below the line?

Sol.

Given:

$$I = 90 \text{ A}$$

$$R = 1.5 \text{ m}$$

Considering Amperian loop and using the above formula

$$B = (2 \times 10^{-7}) \cdot (90) / 1.5$$

Or $B = 1.2 \times 10^{-5} \text{ T}$
Direction is towards south.

4.5. What is the magnitude of magnetic force per unit length on a wire carrying a current of 8 A and making an angle of 30° with the direction of a uniform magnetic field of 0.15 T?

Sol.

Given:

$$I = 8 \text{ A}$$

$$\text{angle} = 30^\circ$$

$$B = 0.15 \text{ T}$$

$$l = 1 \text{ m}$$

The force is given by

$$F = I.l.B.\sin\theta$$

Or $F = 8 \times 1 \times 0.15 \times 0.5$

Or $F = 0.6 \text{ N / m}$

4.6. A 3.0 cm wire carrying a current of 10 A is placed inside a solenoid perpendicular to its axis. The magnetic field inside the solenoid is given to be 0.27 T. What is the magnetic force on the wire?

Sol.

Given:

$$l = 3 \text{ cm}$$

$$I = 10 \text{ A}$$

$$B = 0.27 \text{ T}$$

$$\theta = 90^\circ$$

Then the force

$$F = I.l.B.\sin \Theta$$

Substituting the values give

$$F = 0.081 \text{ N}$$

4.7. Two long and parallel straight wires A and B carrying currents of 8.0 A and 5.0 A in the same direction are separated by a distance of 4.0 cm. Estimate the force on a 10 cm section of wire A.

Sol.

Given:

$$I_a = 8 \text{ A}$$

$$I_b = 5 \text{ A}$$

$$d = 4 \text{ cm}$$

$$L = 10 \text{ cm}$$

Force of wire A

$$F = \frac{\mu_0 I_a I_b L}{2\pi d}$$

Or

$$F = 2 \times 10^{-5} \text{ N}$$

4.8. A closely wound solenoid 80 cm long has 5 layers of windings of 400 turns each. The diameter of the solenoid is 1.8 cm. If the current carried is 8.0 A, estimate the magnitude of B inside the solenoid near its centre.

Sol.

Given:

$$L = 80 \text{ cm}$$

$$N = 2000$$

$$r = 0.9$$

$$I = 8 \text{ A}$$

$$\text{Enclosed current } I_e = 8 \times 2000 = 16000 \text{ A}$$

$$\text{Since, } BL = \mu_o I_e$$

Putting the values

$$B = \mu_o \cdot 16000 / 0.8 = 0.025 \text{ T}$$

4.9. A square coil of side 10 cm consists of 20 turns and carries a current of 12 A. The coil is suspended vertically and the normal to the plane of the coil makes an angle of 30° with the direction of a uniform horizontal magnetic field of magnitude 0.80 T. What is the magnitude of torque experienced by the coil?

Sol.

Given:

$$L = 10 \text{ cm}$$

$$N = 20$$

$$I = 12 \text{ A}$$

$$\Theta = 30^\circ$$

$$B = 0.8 \text{ T}$$

We know

$$\text{Torque} = mB \cdot \sin \Theta$$

$$\text{Or } T = NIAB \sin \Theta$$

$$\text{Or } T = 20 \times 12 \times 0.1 \times 0.1 \times 0.8 \times 0.5$$

$$\text{Or } T = 0.96 \text{ Nm}$$

4.10. Two moving coil meters, M1 and M2 have the following particulars:

$$R_1 = 10 \, \Omega, N_1 = 30,$$

$$A_1 = 3.6 \times 10^{-3} \text{ m}^2, B_1 = 0.25 \text{ T}$$

$$R_2 = 14 \, \Omega, N_2 = 42,$$

$$A_2 = 1.8 \times 10^{-3} \text{ m}^2, B_2 = 0.50 \text{ T}$$

(The spring constants are identical for the two meters).

Determine the ratio of

- a) current sensitivity and
- b) Voltage sensitivity of M2 and M1.

Sol.

Given:

Details of M1

$$R_1 = 10 \text{ ohms}$$

$$N_1 = 30$$

$$A_1 = 3.6 \times 10^{-3} \text{ m}^2$$

$$B_1 = 0.25 \text{ T}$$

Details of M2

$$R_2 = 14 \text{ ohms}$$

$$N_2 = 42$$

$$A_2 = 1.8 \times 10^{-3} \text{ m}^2$$

$$B_2 = 0.5 \text{ T}$$

- a) Current sensitivity of M

$$= N_1 \cdot A_1 \cdot B_1 / k$$

Current sensitivity of M2

$$= N_2 \cdot A_2 \cdot B_2 / k$$

Ratio of current sensitivity

$$= N_2 A_2 B_2 / N_1 A_1 B_1 \text{ (since } k \text{ is identical)}$$

$$= 0.0378 / 0.027$$

$$= 1.4$$

Thus ratio of current sensitivity of M2 and M1 is 1.4

- b) Voltage sensitivity of M1

$$= N_1 \cdot A_1 \cdot B_1 / k \cdot R_1$$

Voltage sensitivity of M2

$$= N_2 \cdot A_2 \cdot B_2 / k \cdot R_2$$

Ratio of voltage sensitivity

$$= N_2 A_2 B_2 R_1 / N_1 A_1 B_1 R_2$$

$$\begin{aligned} &= 0.378 / 0.378 \\ &= 1 \end{aligned}$$

Thus ratio of voltage sensitivity of M2 and M1 is 1.

4.11. In a chamber, a uniform magnetic field of 6.5 G ($1 \text{ G} = 10^{-4} \text{ T}$) is maintained. An electron is shot into the field with a speed of $4.8 \times 10^6 \text{ m s}^{-1}$ normal to the field. Explain why the path of the electron is a circle. Determine the radius of the circular orbit. ($e = 1.6 \times 10^{-19} \text{ C}$, $m_e = 9.1 \times 10^{-31} \text{ kg}$)

Sol.

Since the electron has velocity perpendicular to magnetic field B , the centripetal force ($q \cdot V \times B$) comes in action and a circular motion is described by electron perpendicular to the magnetic field.

Its radius is given by

$$r = mv / qB$$

Here

$$m = 9.1 \times 10^{-31} \text{ kg}$$

$$v = 4.8 \times 10^6 \text{ m / s}$$

$$q = 1.6 \times 10^{-19} \text{ C}$$

$$B = 6.5 \times 10^{-4} \text{ T}$$

Substituting the values we get

$$r = 0.042 \text{ m}$$

4.12. In Exercise 4.11 obtain the frequency of revolution of the electron in its circular orbit. Does the answer depend on the speed of the electron? Explain.

Sol.

Frequency of revolution, $w = v / r$
Or $2\pi f = 4.8 \times 10^6 / 0.042$
Or $f = 18 \text{ MHz}$
Frequency is independent of velocity.

4.13.

- a) A circular coil of 30 turns and radius 8.0 cm carrying a current of 6.0 A is suspended vertically in a uniform horizontal magnetic field of magnitude 1.0 T. The field lines make an angle of 60° with the normal of the coil. Calculate the magnitude of the counter torque that must be applied to prevent the coil from turning.
- b) Would your answer change, if the circular coil in (a) were replaced by a planar coil of some irregular shape that encloses the same area? (All other particulars are also unaltered.)

Sol.

Given:

$$N = 30$$

$$r = 8 \text{ cm}$$

$$I = 6 \text{ A}$$

$$B = 1 \text{ T}$$

$$\Theta = 60^\circ$$

- a) We know

$$\text{Torque} = NIAB \sin \Theta$$

Substituting the values

$$\text{Torque} = 3.13 \text{ Nm}$$

- b) No, the torque does not depend on configuration of loop.